

Estimation and diagnosis of  
analysis/background errors  
using ensemble assimilation

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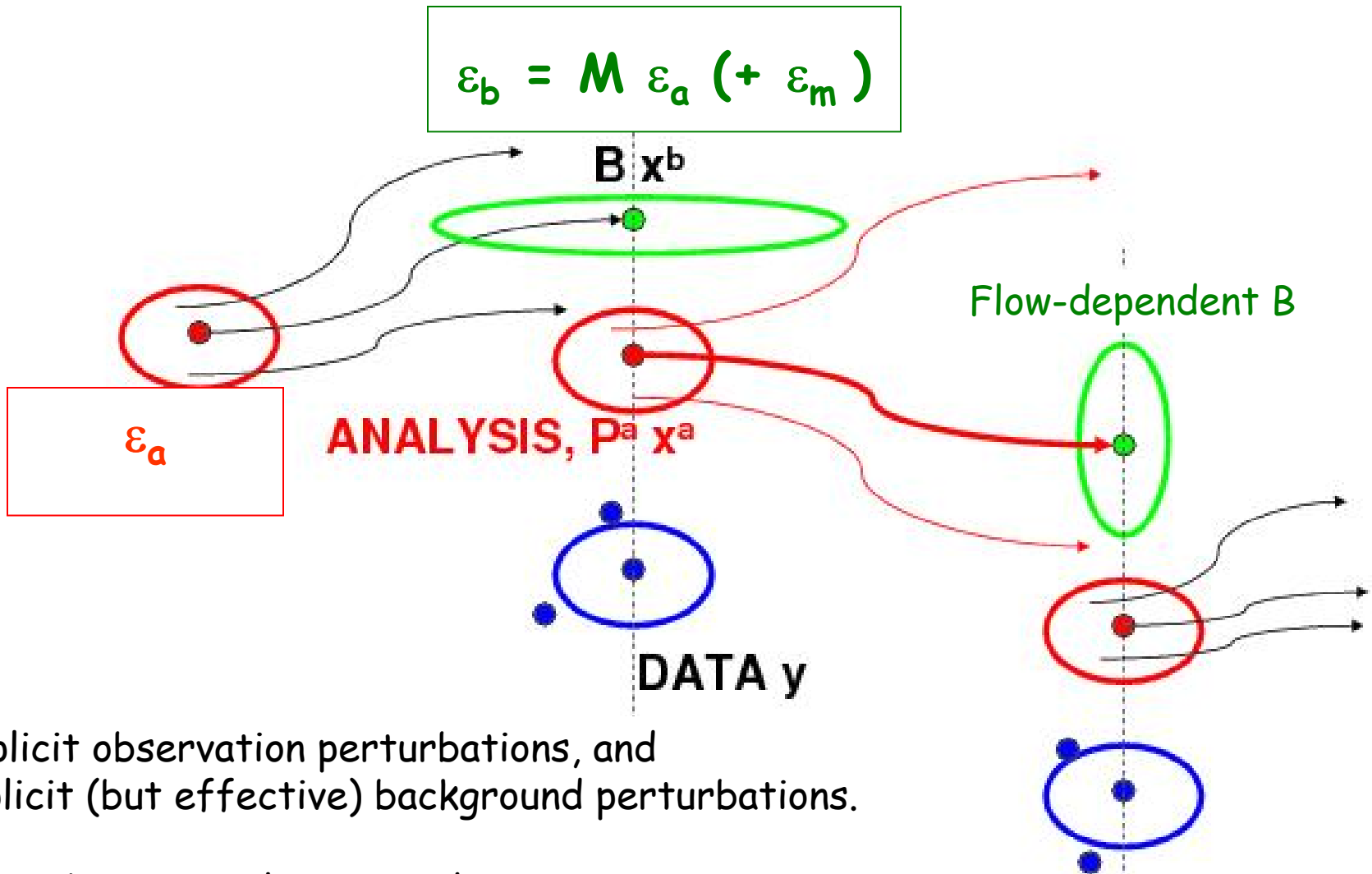
*Thanks to Gérald Desroziers*



# Outline

1. Simulation of the error evolution
2. The operational MF ensemble variational assimilation
3. Diagnostics of analysis and background errors
4. Combined use of innovation-based and EnDA estimates

# Ensemble assimilation (EnDA = EnVar, EnKF, ...) : simulation of the error evolution



(Houtekamer et al 1996; Fisher 2003 ;  
Ehrendorfer 2006 ; Berre et al 2006)

# The analysis error equation

(e.g. Daley 1991, Berre et al 2006)

Analysis state :

$$x_a = (I-KH) x_b + K y$$

True state (with  $y^* = H x^*$ ):

$$x_* = (I-KH) x_* + K y_*$$

Analysis error :

$$e_a = (I-KH) e_b + K e_o$$

with

$$e_a = x_a - x_*$$

This is true even if  $K$  is suboptimal. NL case ok too.

# The analysis perturbation equation

Perturbed analysis :

$$x'_a = (I-KH) x'_b + K y'$$

Unperturbed analysis :

$$x_a = (I-KH) x_b + K y$$

Analysis perturbation :

$$\varepsilon_a = (I-KH) \varepsilon_b + K \varepsilon_o$$

with

$$\varepsilon_a = x'_a - x_a$$

# Formal comparison with NMC method

(Bouttier 1994, Berre et al 2006)

Analysis error : 
$$e_a = (\mathbf{I}-\mathbf{KH}) e_b + \mathbf{K} e_o$$

Analysis perturbation (EnDA) : 
$$\varepsilon_a = (\mathbf{I}-\mathbf{KH}) \varepsilon_b + \mathbf{K} \varepsilon_o$$

Analysis increment (NMC) : 
$$dx = -\mathbf{KH} e_b + \mathbf{K} e_o$$

with  $\mathbf{I}-\mathbf{KH} \sim$  high-pass filter, whereas  $\mathbf{KH} \sim$  low-pass filter.

⇒ Sharper correlations in EnDA than in NMC  
(e.g. Belo Pereira and Berre 2006, Fisher 2003).

⇒ Better simulation of the analysis error equation in EnDA than in NMC.

# Simulation of the error evolution : open issue(s)

Ex: reference 4D-Var and +/- high resolution model.

Possible approximations in the ensemble :

- reduce **horizontal resolution** of the model.
  - approximate reference **4D-Var gain matrix K**, with :
    - 3D-Fgat,
    - 4D-Var and fewer outer loops,
    - ETKF/EnKF : by deriving K from the ensemble « only ».
- ⇒ What is the best approach (for a given computation cost) ?
- EnKF-Var** hybrid approaches : the « hybrid K » is not accounted for in the analysis perturbation update (in contrast with « consistent **EnVar** »).
- (**model error** representation...)

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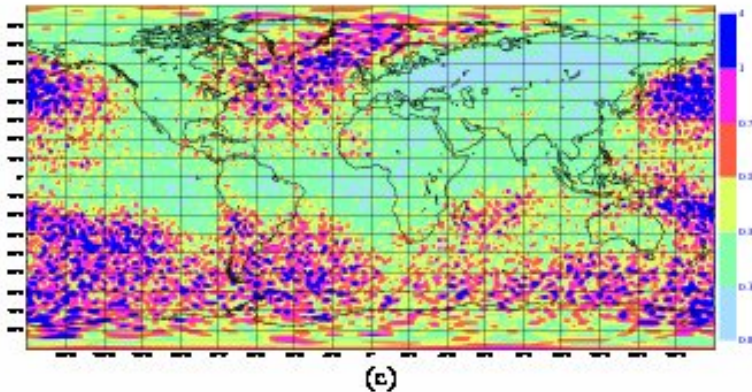
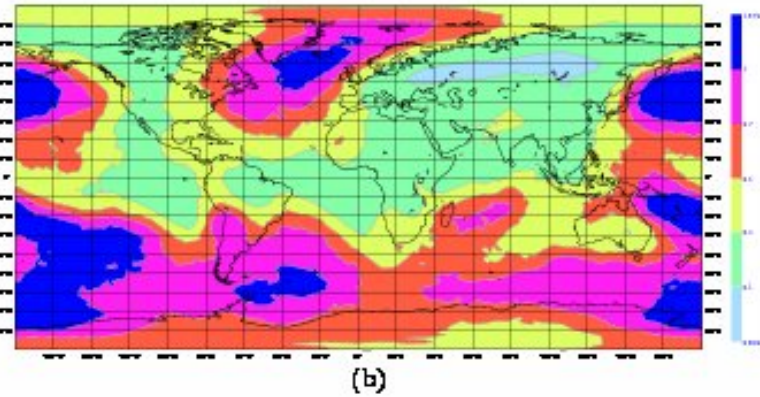
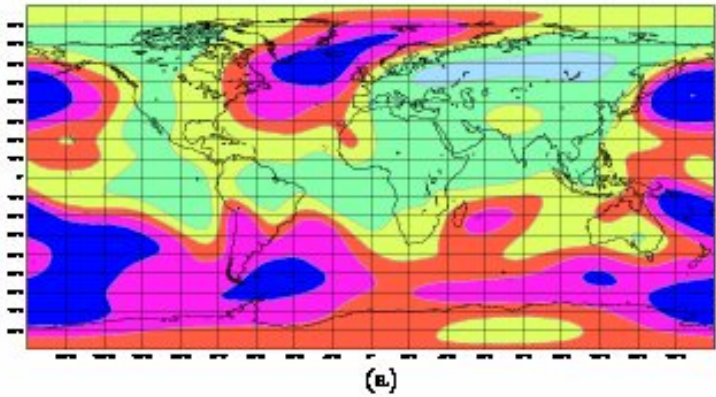
# The operational MF ensemble Var assimilation

- 6 perturbed global members T359 L60 with 3D-Fgat (Arpege).
- **Spatial filtering** of error variances (see later), to further increase sample size and robustness (~90%).
- **Inflation** of ensemble B (by  $1.3^2$ ), as in the static approach, to represent model error contributions.
- The Arpege 4D-Var uses these «  $\sigma$ 's of the day ». ⇒ **operational** since July 2008.
- Off-line coupling with six **LAM** members, with both Aladin (10 km) and Arome (2.5 km).

# “OPTIMIZED” SPATIAL FILTERING OF THE SIGMAB FIELD

« TRUE » SIGMAB'S

**FILTERED** SIGMAB's (N = 6)



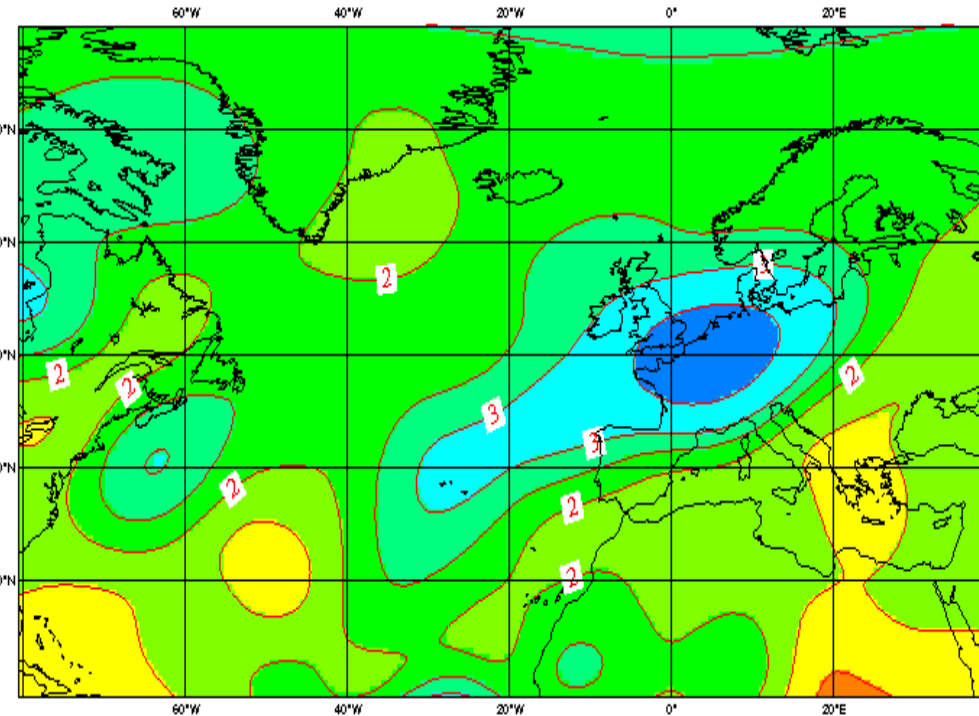
**RAW** SIGMAB's (N = 6)

$$\varepsilon_b = B^{1/2} \eta$$

$$V_b^* \sim \rho V_b$$

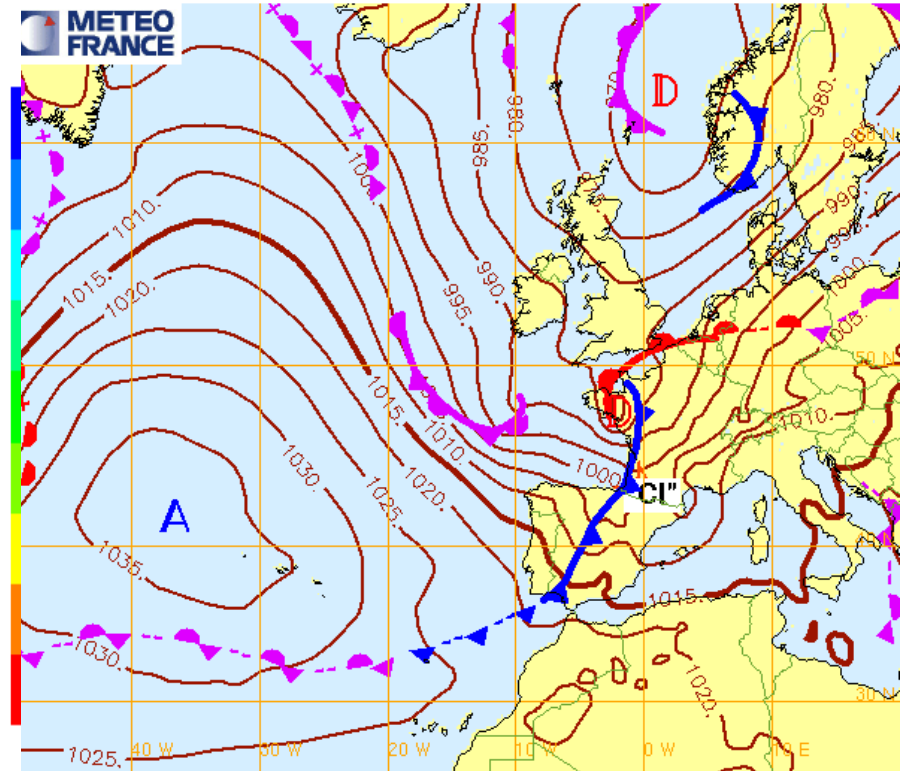
(Raynaud et al 2008)

# Connection between large sigmab and intense weather ( 08/12/2006 , 03-06UTC )



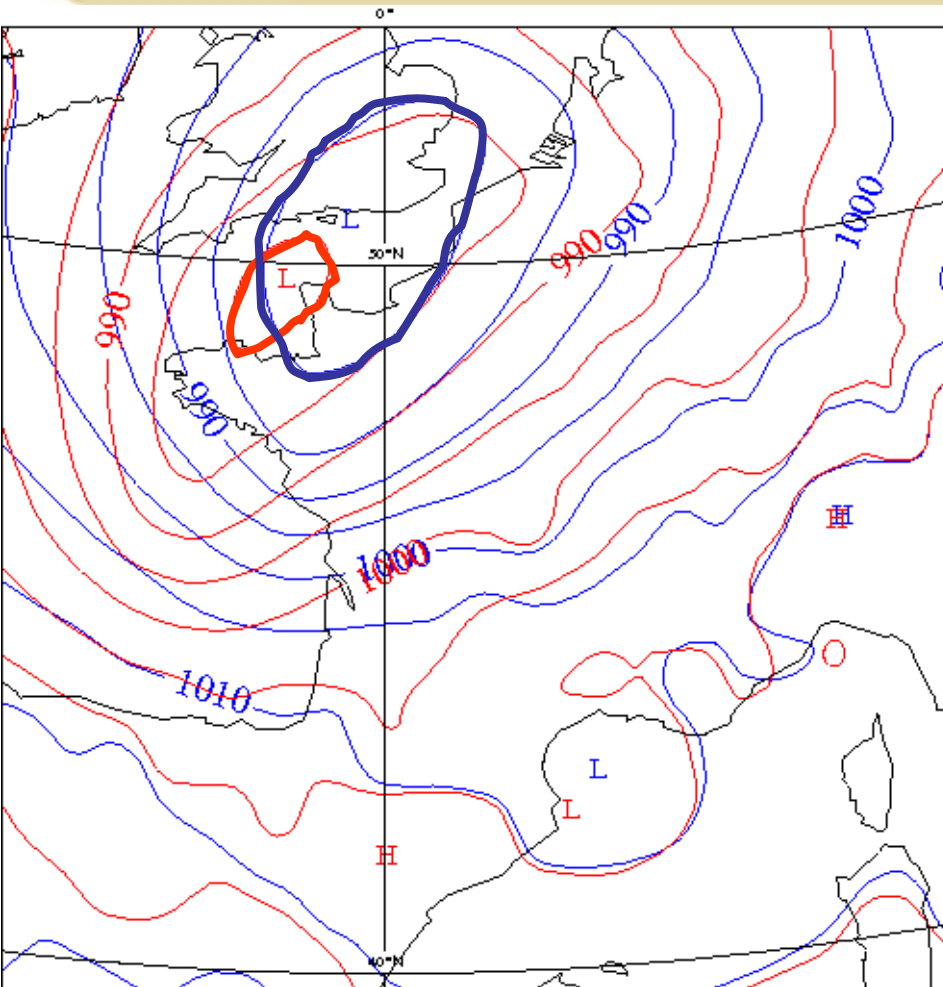
**Ensemble spread:  
large sigmab over France**

analyse Fronts et isobares du 08/12/2006 06hUTC (reseau: 08/12/2006 06hUTC)

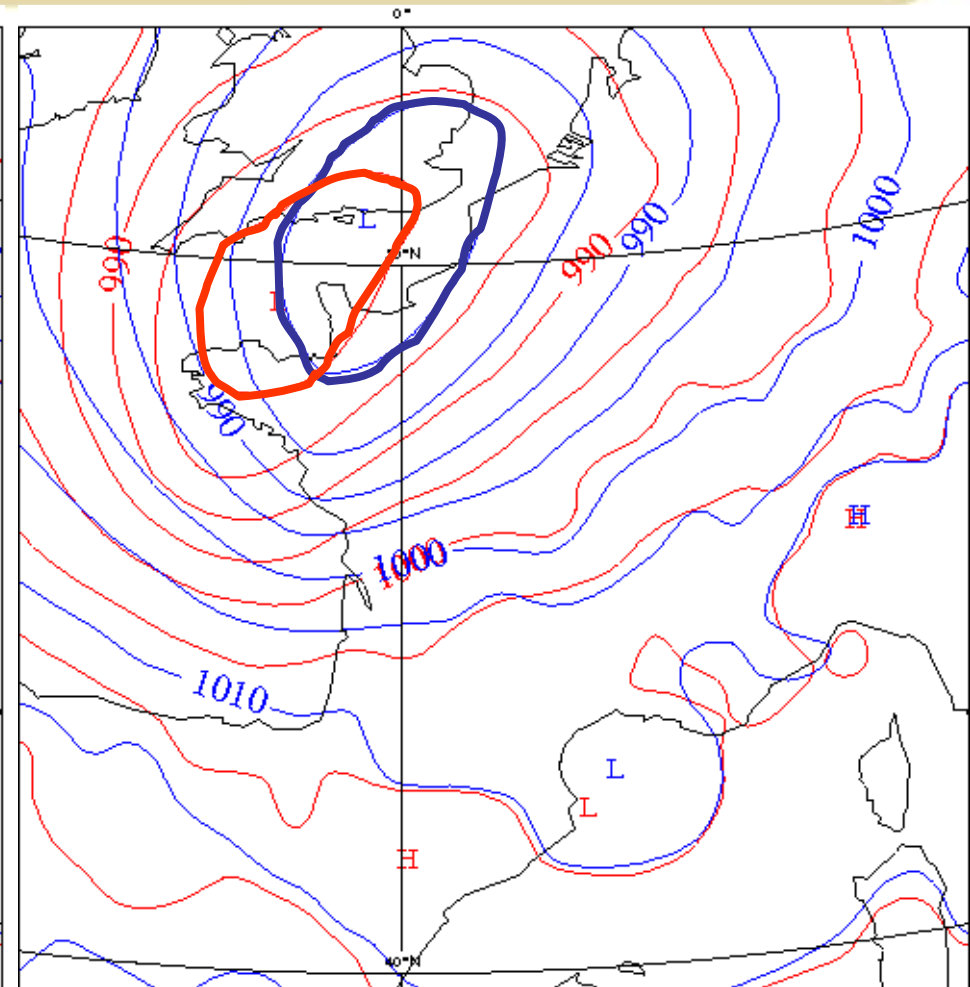


**Mean sea level pressure :  
storm over France**

# Impact on a severe storm (10/02/2009) : 36h forecasts versus verifying analysis



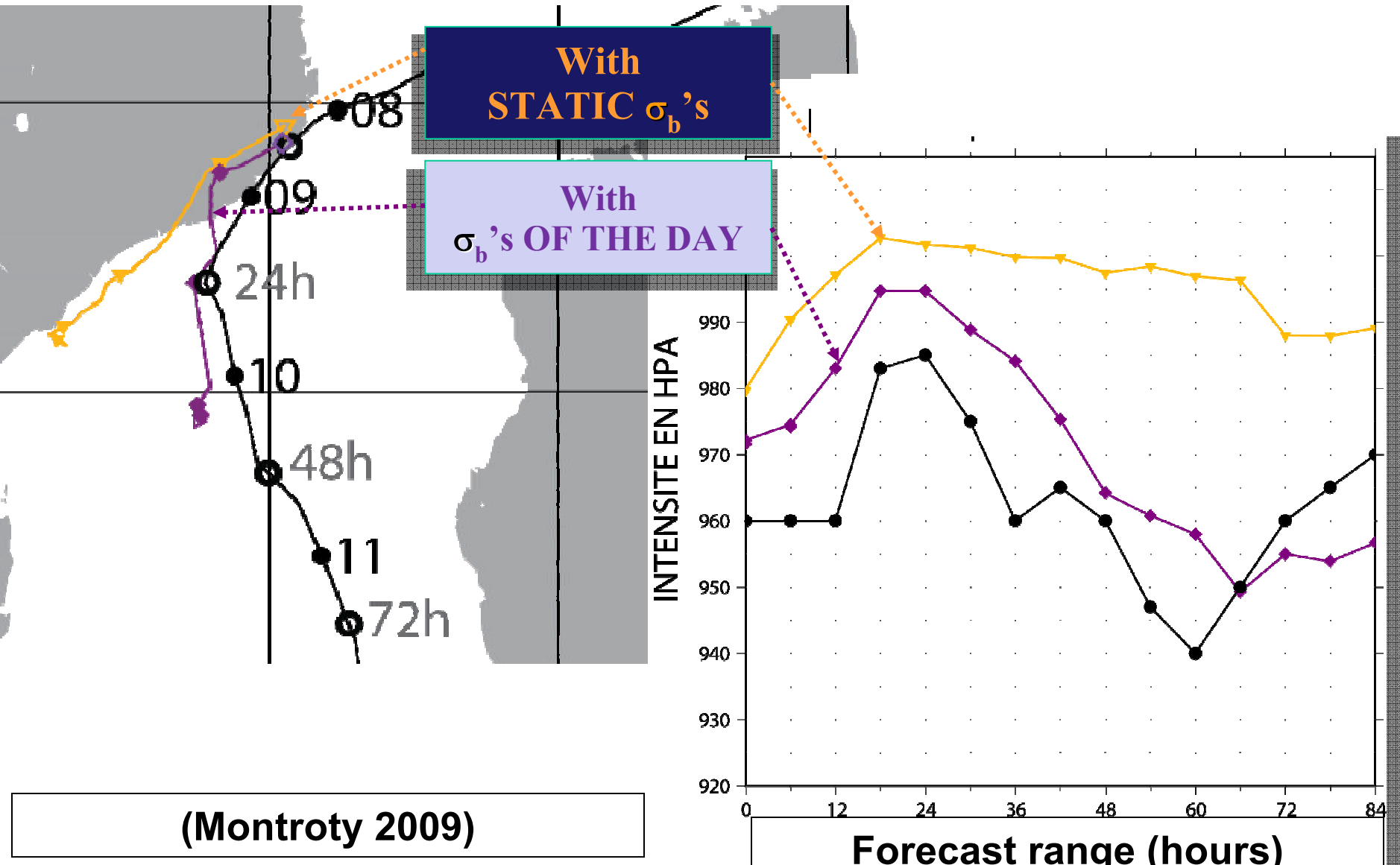
With climatological  $\sigma_b$ 's



With  $\sigma_b$ 's « of the day »

⇒ Positive impact on the depth of the low + gradient intensity

# Impact of $\sigma_b$ « of the day » on the forecast of cyclone *Jokwe*



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# Analysis and background errors

- Analysis error estimate in the **optimal** case :

$$A = (I - KH) B$$

⇒ Analysis errors expected to be smaller than background errors.

- Analysis error estimate in the **more general case (suboptimal), with EnDA** :

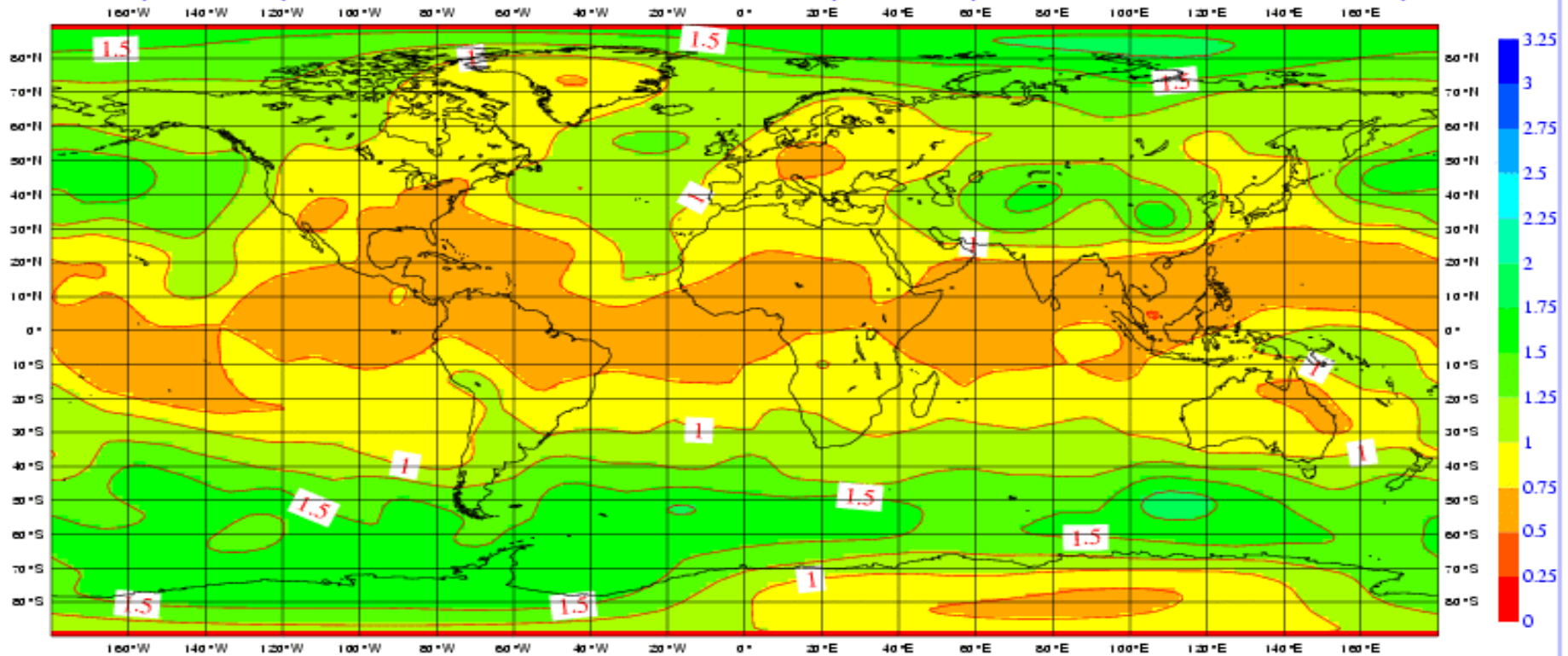
$$A = (I - KH) B (I - KH)^T + K R K^T$$

⇒ Compare ensemble-based estimates of  $A$  and  $B$  to diagnose analysis effects.



# Background error standard deviations (vorticity, 500 hPa)

Thursday 28 February 2002 02UTC ECMWF Forecast t+6 VT: Thursday 28 February 2002 08UTC Model Level 20 \*\*vorticity

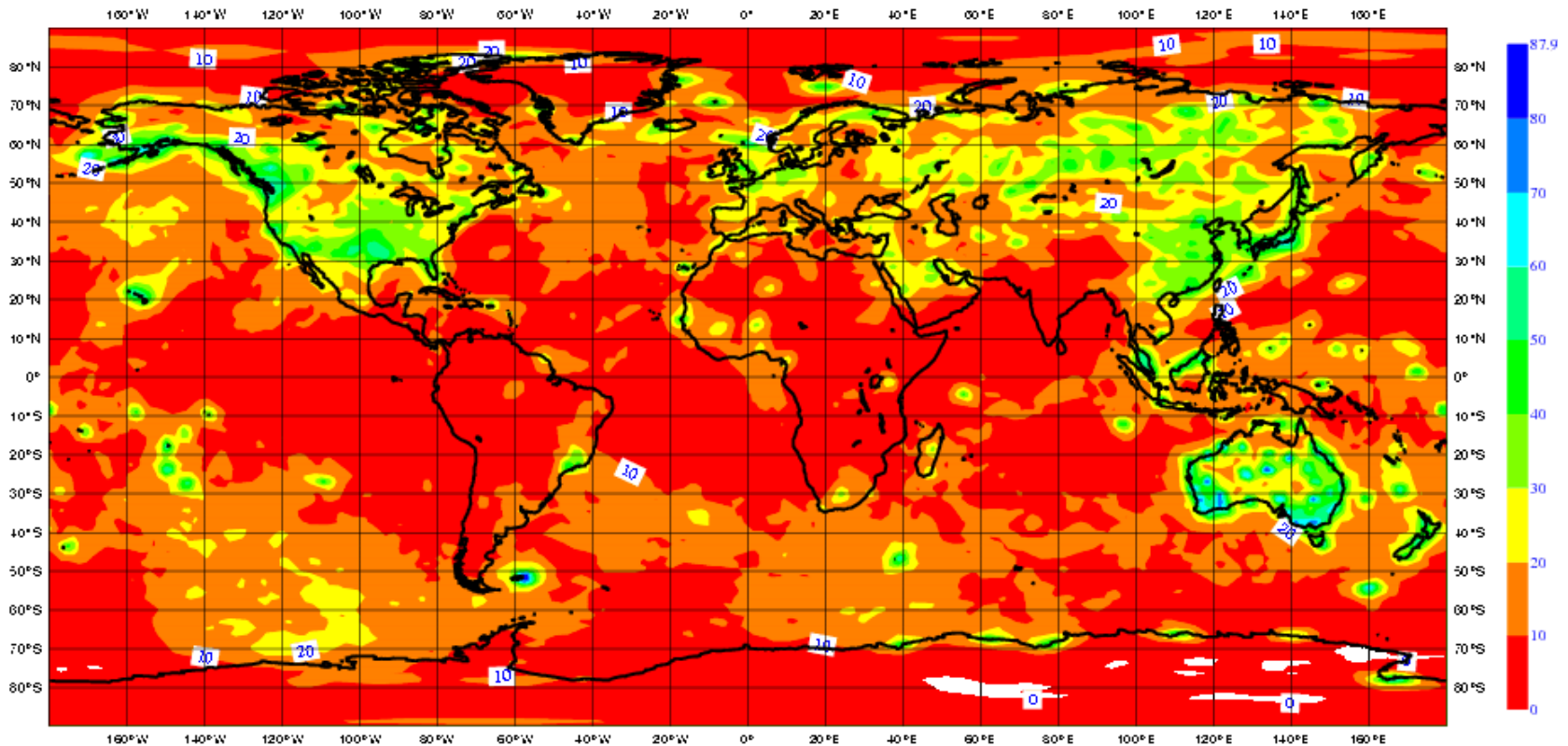


One month-averaged standard deviations (February 2002)

(Belo Pereira and Berre 2006)



# Ensemble $\sigma^b - \sigma^a$ with energy norm

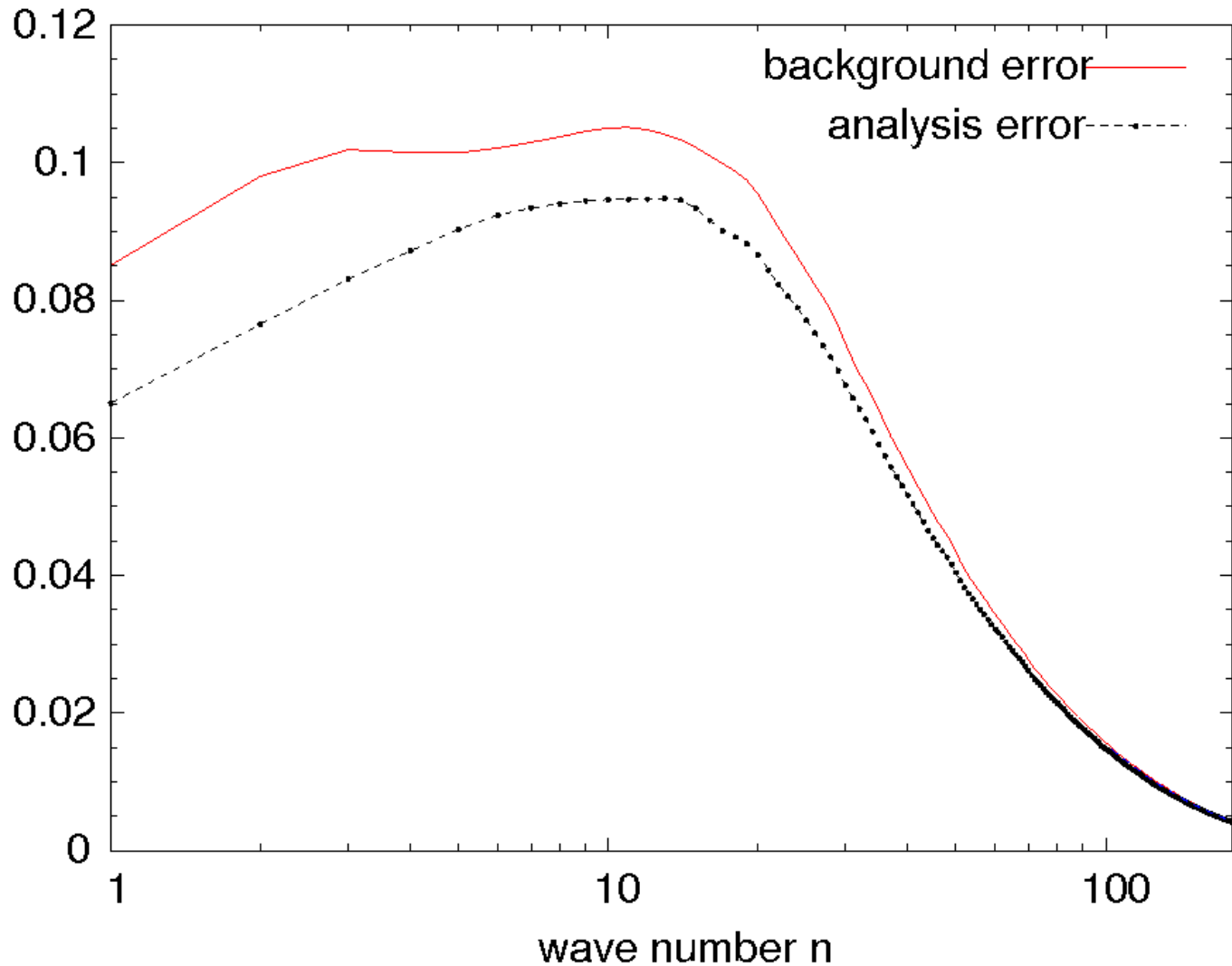


One month statistics (January 2007) at 00UTC

(Desroziers, pers. comm.)

# Power spectra of error variances

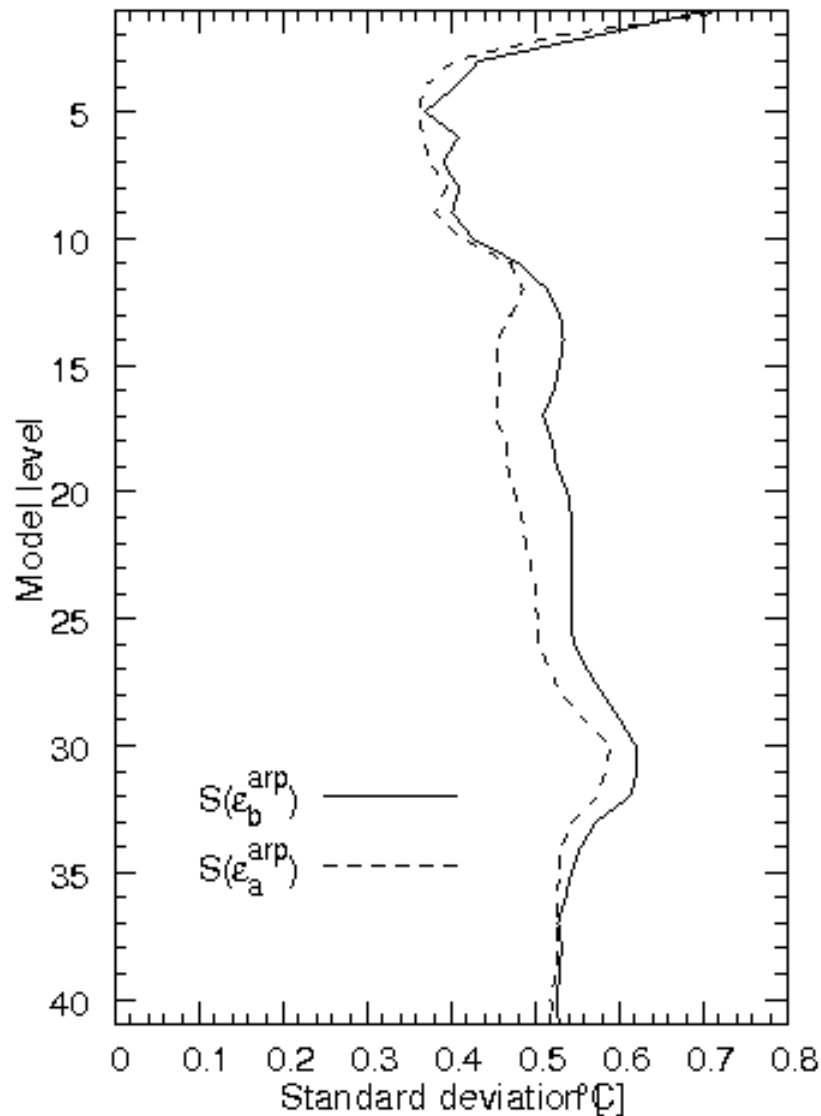
(Stefanescu et al 2006, Belo Pereira and Berre 2006)



ERROR  
STD DEVIATION

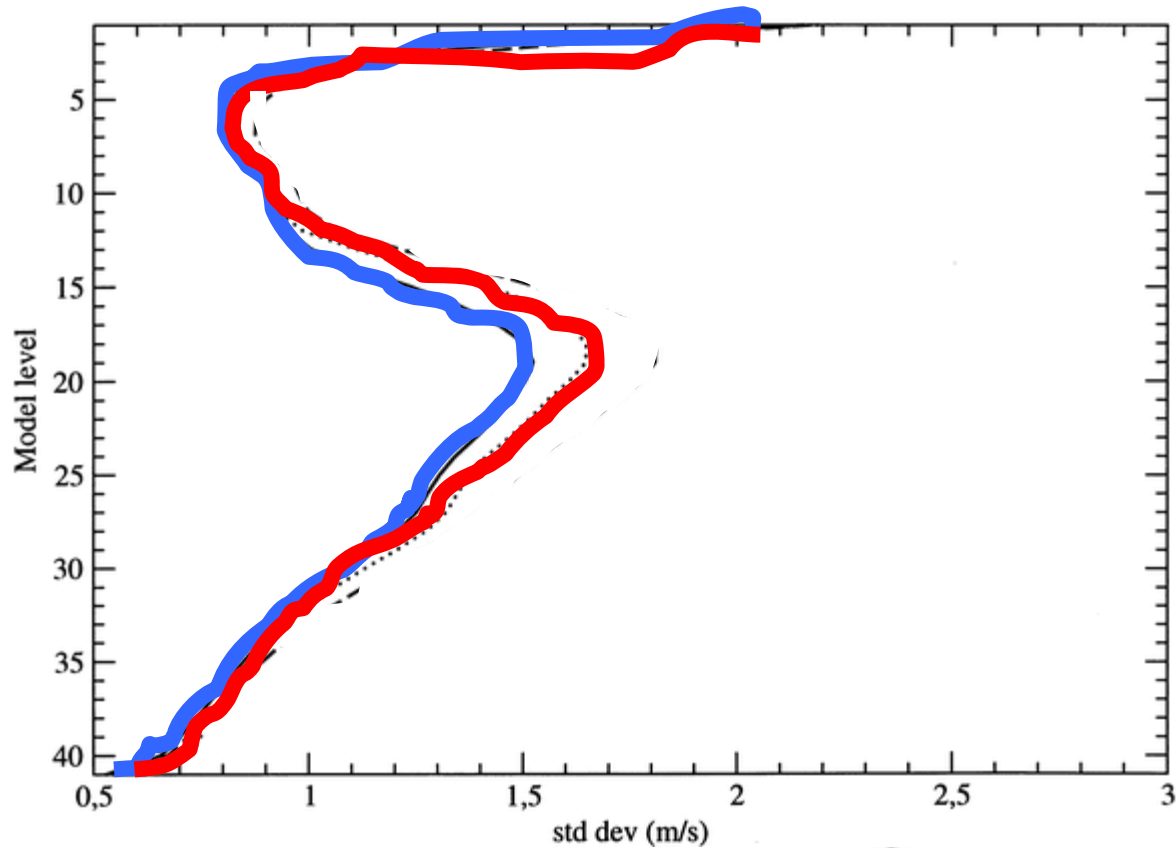
**Analysis effect:**  
reduction of large-scale component of background errors, in particular in data-rich regions.

# Vertical profile of temperature error standard deviations

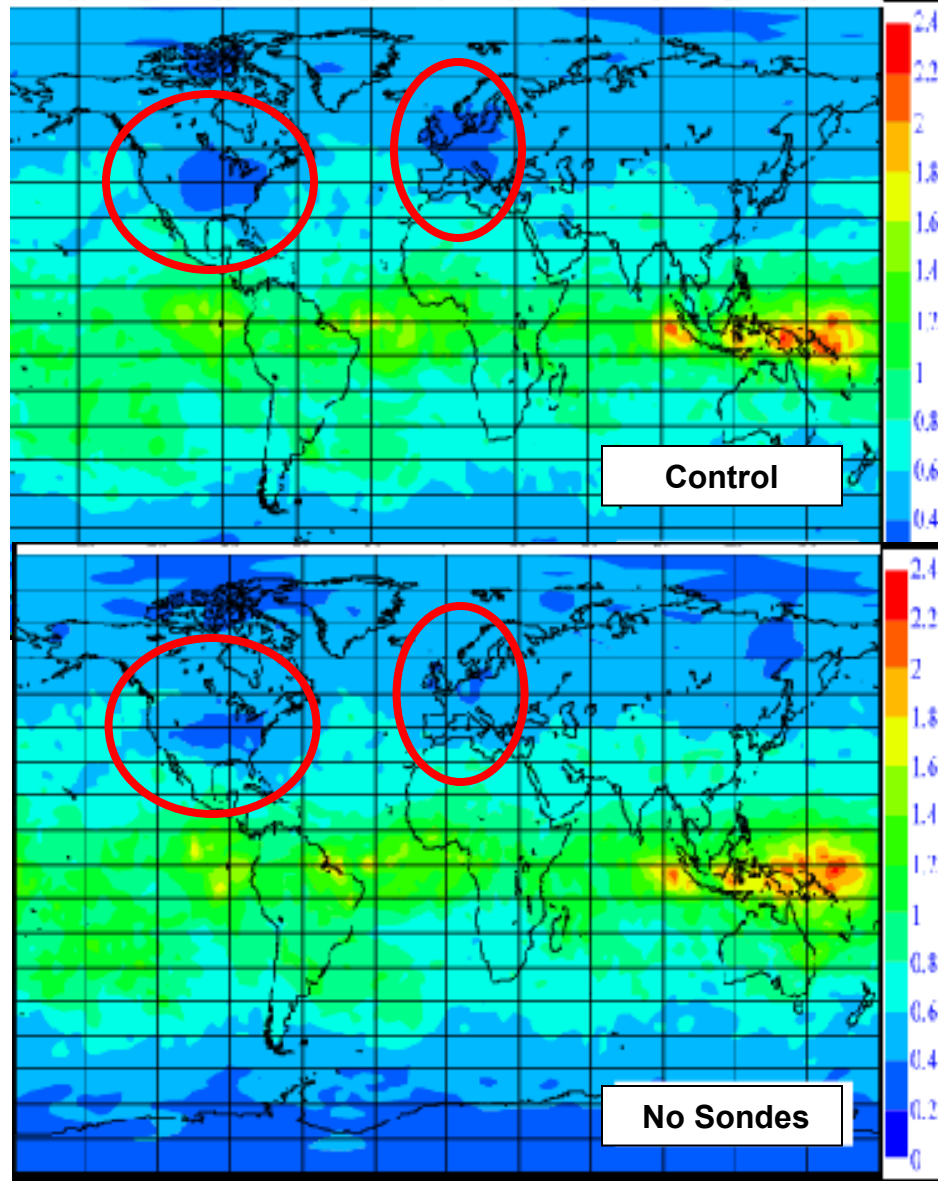


# Analysis errors and forecast errors

(Belo Pereira and Berre 2006)



# Impact of radiosondes on ensemble analysis spread ( $\sigma_a$ )



(Andersson, Tan et al 2005)

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# Innovation-based sigma estimate (Desroziers et al 2005)

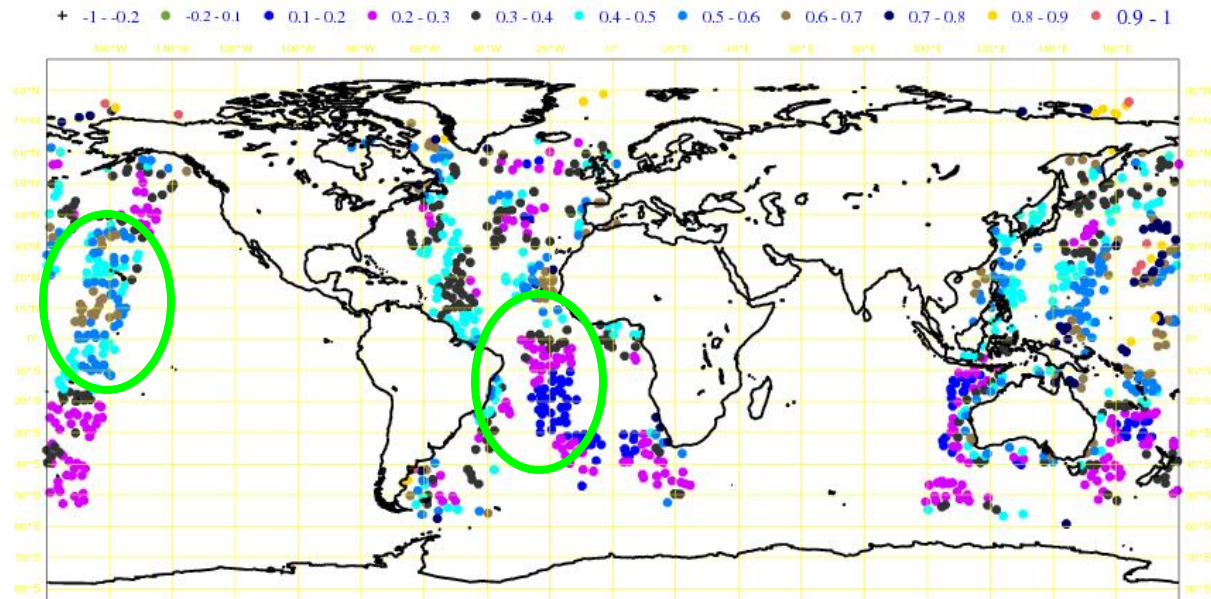
$$\text{cov}( H dx , dy ) \sim H B H^T$$

- ⇒ This can be calculated **for a specific date**,  
to examine flow-dependent features, but then the  
local sigma is calculated from **a single error realization** (  $N = 1$  )!
- ⇒ Conversely, if we calculate **local spatial averages** of these sigma's,  
the sample size will be increased, and  
**comparison with ensemble can be considered.**



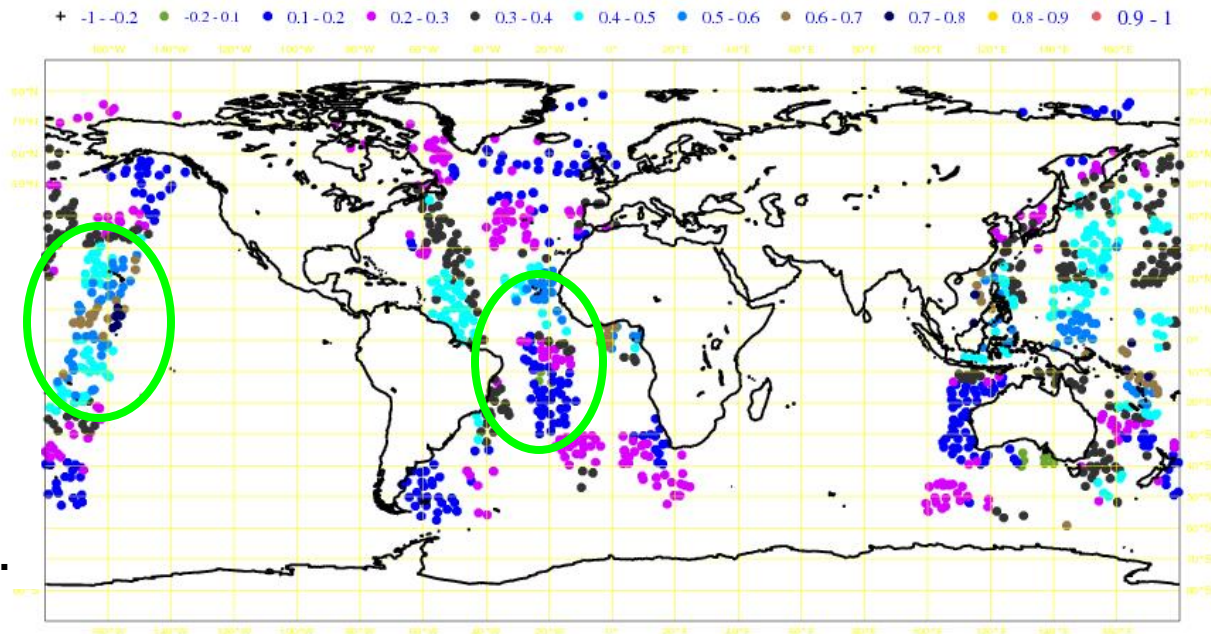
# Validation of ensemble sigma-b's « of the day » HIRS 7 (28/08/2006 00h)

Ensemble sigma-b's



« Observed » sigma-b's  
 $\text{cov}(H dx, dy) \sim H B H^T$   
(Desroziers et al 2005)

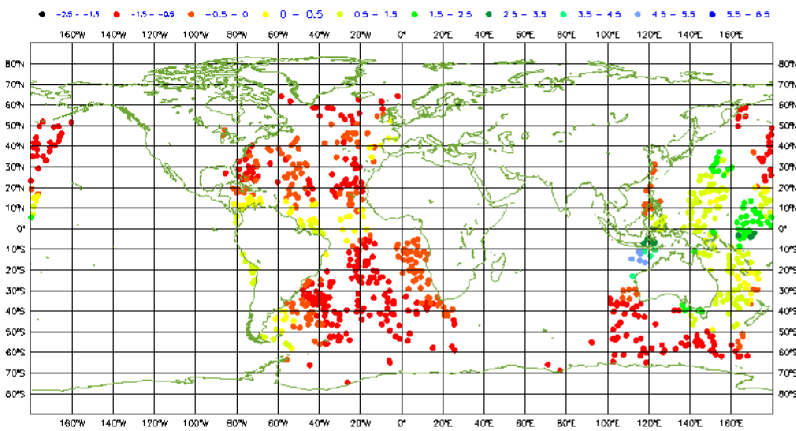
=> model error estimation.



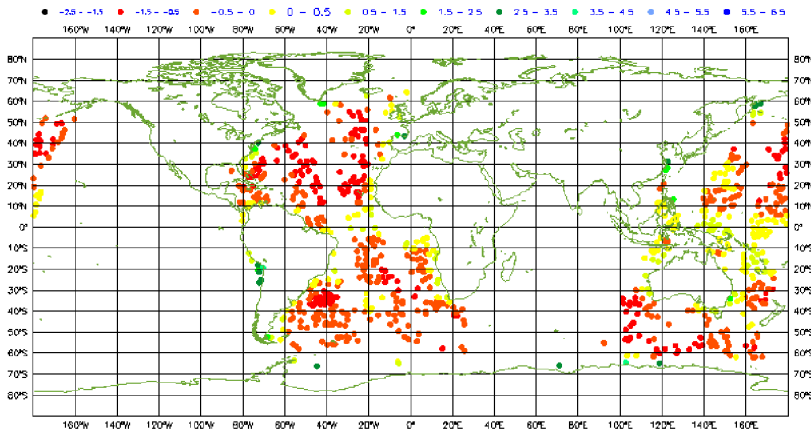


# Estimates of $\sigma_b$ of the day, in HIRS 7 space

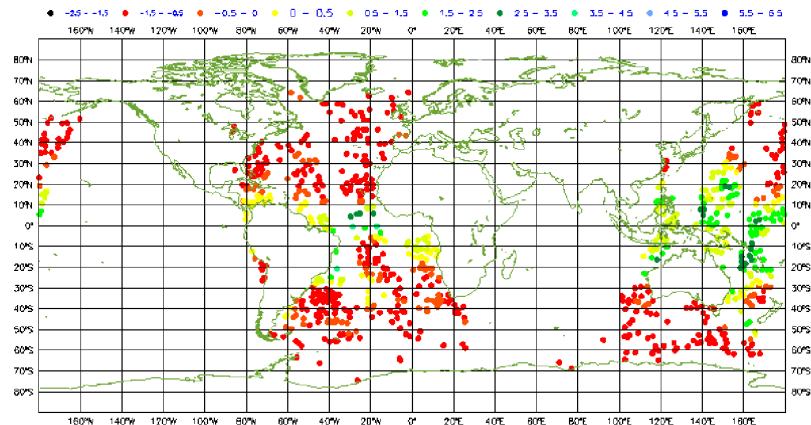
cov( H dx , dy ) of 4D-Var



(a) HIRS7-diagnostic



(b) HIRS7-63HE-HR



Ensemble 3D-Fgat

Ensemble 4D-Var

(from Gibier, 2009)

# Method(s) for estimating model error covariances (Q)

$$B = MAM^T + Q$$

- Use **EnDA** to estimate «  $MAM^T$  ».
- Use **innovation diagnostics** to estimate «  $B$  » (or at least  $HBH^T$ ).
- Estimate **Q** as :

$$Q \sim B - MAM^T$$

(e.g. **Daley 1992**)

# Conclusions

- EnDA allows **analysis/background error cycling** to be simulated and diagnosed.
- Diagnostic comparison between analysis and background spread provides **information about analysis effects**.
- Comparisons with **innovation diagnostics** :  
for validation, and for estimation of model error covariances.
- **Flow-dependent covariances** can be estimated,  
with a positive impact on intense/severe weather events.
- **Open issues** : optimization of error simulation, covariance estimation/filtering,  
and implementation techniques in 3D/4D-Var.



Thank you  
for your attention



# Background, analysis and forecast errors

(Belo Pereira and Berre 2006)

